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Citation

Roper, M., R. E. Pepper, M. P. Brenner, and A. Pringle. 2008. "Explosively Launched Spores of Ascomycete Fungi Have Drag-Minimizing Shapes." *Proceedings of the National Academy of Sciences* 105 (52) (December 22): 20583–20588. doi:10.1073/pnas.0805017105.

Published Version

doi:10.1073/pnas.0805017105

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Explosively launched spores of ascomycete fungi have drag-minimizing shapes

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Edited by Alexandre J. Chorin, University of California, Berkeley, CA, and approved September 8, 2008 (received for review May 23, 2008)

The forcibly launched spores of ascomycete fungi must eject through several millimeters of nearly still air surrounding fruiting bodies to reach dispersive air flows. Because of their microscopic size, spores experience great fluid drag, and although this drag can aid transport by slowing sedimentation out of dispersive air flows, it also causes spores to decelerate rapidly after launch. We hypothesize that spores are shaped to maximize their range in the nearly still air surrounding fruiting bodies. To test this hypothesis we numerically calculate optimal spore shapes—shapes of minimum drag for prescribed volumes—and compare these shapes with real spore shapes taken from a phylogeny of >100 species. Our analysis shows that spores are constrained to remain within 1% of the minimum possible drag for their size. From the spore shapes we predict the speed of spore launch, and confirm this prediction through high-speed imaging of ejection in *Neurospora tetrasperma*. By reconstructing the evolutionary history of spore shapes within a single ascomycete family we measure the relative contributions of drag minimization and other shape determinants to spore shape evolution. Our study uses biomechanical optimization as an organizing principle for explaining shape in a mega-diverse group of species and provides a framework for future measurements of the forces of selection toward physical optima.

hydrodynamics | biological optimization | fungal spores

Many organisms have visible adaptations for minimizing drag, including the streamlined shapes of fast-swimming fish and of Mayfly nymphs that cleave to rocks in rapidly flowing streams, or the precisely coordinated furling of tulip tree leaves in strong winds (1). However, although drag minimization may improve some aspects of individual fitness, it is also clear that physiological and ecological trade-offs will constrain the evolution of body shape. Similarly, although signatures of optimization can be seen in diverse features of organism morphology (2), behavior (3), and resource allocation (4, 5), the strength of the force of selection for one physical optimum over another can not be readily quantified (6).

Most fungi grow on highly heterogeneous landscapes and must move between disjoint patches of suitable habitat. Sexual spores can be carried by air flows and allow dispersal between patches (7, 8). To reach dispersive air flows, spores of many species of ascomycete fungi are ejected from asci, fluid-filled sacs containing the spores (9). At maturity the turgor pressure within each sac climbs until a critical pressure is reached, whereupon a hole opens at the apex and spores are ejected (8). Spores must travel far enough from the originating fruiting body to enter dispersive air flows. In particular, it is necessary that they pass through a boundary layer of still air of thickness ~ 1 mm that clings to the fungal fruiting body (10).

Multiple independently evolved adaptations enhance spore range in disparate fungal species. For example, appendages and mucilaginous sheaths promote spore cohesion during launch, increasing projectile mass but allowing spores to subsequently disassociate into small, easily dispersed fragments (7, 11), whereas the long thread-like spores of some Sordariomycete fungi are ejected slowly and may physically span the layer of still air before

fully leaving the ascus (12). We consider how spores lacking these conspicuous adaptations may yet be shaped to maximize range.

We analyze an entire phylogeny of >100 such species for drag minimization. We use numerical optimization to construct drag-minimizing shapes over the range of flow speeds and sizes relevant to real spores. These drag-minimizing shapes are very different from the well understood forms of macrobodies such as man-made projectiles and fast-swimming animals (13). By comparing real spores with these optimal shapes we predict the speed of spore ejection, and then confirm this prediction through high-speed imaging of ejection in *Neurospora tetrasperma*.

A simple physical argument shows that the speed of ejection of unappendaged spores is itself insensitive to spore shape, size, or species identity. We can estimate the speed of a launched spore by noting that during ejection, the work of the turgor pressure ($\Delta p V$, where V is the volume of a spore) is converted to kinetic energy, giving the spore a velocity

$$U_0 = \sqrt{\frac{2\Delta p}{\rho}}, \quad [1]$$

which depends on the density, $\rho \approx 1,200 \text{ kg}\cdot\text{m}^{-3}$ (7), of the spore but not on its shape or size. Furthermore, assuming that the ascus is inflated to the largest overpressure allowed by the concentration and activity of the osmolytes present (14), we expect Δp , and thus U_0 , to be conserved across all ascomycetes with explosive spore ejection.

The speed of ejection has not been directly measured for any singly ejected, unappendaged ascomycete spore, but is constrained by previous indirect measurements. The turgor pressure within a ripe ascus has been estimated to be $\Delta p \approx 0.08\text{--}0.3 \text{ MPa}$ (16); from which Eq. 1 would give $U_0 = 10\text{--}20 \text{ m}\cdot\text{s}^{-1}$. Such pressure-based estimates give only upper bounds on U_0 , they neglect the friction between spore and ascus walls. Spore travel distances are similarly strongly affected by air flows but give a second set of upper bounds ranging between $9\text{--}35 \text{ m}\cdot\text{s}^{-1}$ (14, 17, 18). Nonetheless, although the value of U_0 is not known, the assumption that launch speed is conserved among species with this mode of ejection is supported by Vogel's remarkable collection of launch speed data for a large range of plant and fungal projectiles (15).

Ingold (7) hypothesized that spores are shaped to maximize the speed of ejection by minimizing frictional losses within the ascus. We find no evidence of selection for such shapes: in the [supporting information \(SI\) Appendix II](#) we analyze a model for friction within the ascus and show that minimization of frictional

Author contributions: M.R., R.E.P., M.P.B., and A.P. designed research; M.R., M.P.B., and A.P. performed research; M.R., M.P.B., and A.P. analyzed data; and M.R., M.P.B., and A.P. wrote the paper.

The authors declare no conflict of interest.

This article is a PNAS direct submission.

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This article contains supporting information online at www.pnas.org/cgi/content/full/0805017105/DCSupplemental.

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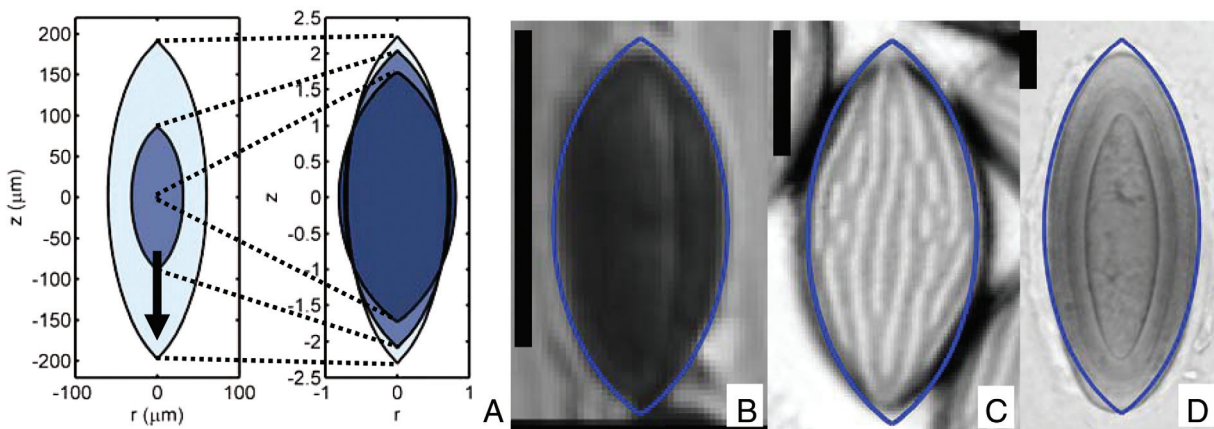


Fig. 1. Real and drag-minimizing spore shapes. (A) Minimal drag shapes for $Re = 0.1$ (darkest), 1, 10 (lightest). The arrow points in the direction of flight and spores are axisymmetric about this direction. (Left) Spore dimensions are given in physical units (assuming $U_0 = 2.1 \text{ m} \cdot \text{s}^{-1}$). (Right) All spores are scaled to have equal volumes. The near fore-aft symmetry is not imposed (20). Comparison of minimal-drag shapes with *Astrocystis cepiformis* (B), *N. crassa* (C), *Pertusaria islandica* (D) spores. (Scale bar: $10 \mu\text{m}$.) Like surface ornamentations (Fig. 2 and Table 1), rounding of spore apices only mildly increases drag. [B, reproduced with permission from ref. 38 (copyright 1998, British Mycological Society); C, reprinted from *Experimental Mycology* Vol 14, Glass NL, Metzzenberg RL, Raju NB, Homothallic Sordariaceae from nature: The absence of strains containing only the a mating type sequence, 16 pp, 2008, with permission from Elsevier; D, reproduced with permission from ref. 39 (copyright 2006, British Lichen Society).]

losses favors oblate shapes. Such shapes are not seen in real spore shape data (see Fig. 3A).

With launch speed conserved, maximizing the spore range requires minimizing the ratio of drag to mass. To see this, balance the fluid drag $-\zeta u$, where u is the speed and ζ is the Stokes drag coefficient, which is approximately independent of speed for sufficiently small projectiles (10), against the inertia of the spore:

$$m \frac{du}{dx} = -\zeta u \Rightarrow x_{\max} \approx \frac{m U_0}{\zeta}, \quad [2]$$

where x is the distance traveled and m is the spore mass. This formula can only be used to infer distance traveled from spore shape for the smallest spores (for which the Reynolds number, Re , defined below, is <1). Although there is no formula relating distance traveled to spore shape for larger spores ($Re > 1$), it is clear, nevertheless, that minimization of the drag-to-mass ratio will maximize the distance traveled by the spore during the early part of its trajectory. In the SI we describe the three assumptions necessary for computing and then minimizing the drag on an ejected spore.

Results and Discussion

Shapes that minimize the ratio of drag to mass can be efficiently computed by using algorithms developed for the design of airplane wings (19): our implementation iteratively modifies the projectile shape, at each iteration solving numerically for the flow field around the shape and then for an adjoint flow field to determine the shape perturbation that gives the largest possible reduction in drag. The algorithm for computing minimum drag shapes is described in ref. 20 and summarized in the *Materials and Methods*. Optimal shapes are parameterized by the *Reynolds number* $Re \equiv U_0 a / \nu$, where ν is the kinematic viscosity of air, and a is the volumetric radius (the radius of a sphere with matching volume) of the spore. Assuming that U_0 does not vary between species, the Reynolds number provides a dimensionless measure of the spore size. For example, $U_0 = 2 \text{ m} \cdot \text{s}^{-1}$ implies $Re = a / (9 \mu\text{m})$. In Fig. 1, minimal drag shapes are displayed for Re ranging from 0.1 up to 10, and compared with real spore shapes.

To determine whether the species shown in Fig. 1B are representative of ascomycetes with explosive ejection, we compared real spores with optimal shapes in over 102 species by using a previously created phylogeny of the phylum Ascomycota (21). Shape data were gathered from 77 species whose spores are launched forcibly and individually. We rejected species whose spores have

adaptations such as appendages or septa, which may have different ejection dynamics (see SI Appendix, Section III). When possible, rejected species were replaced by species within the same genus lacking any such adaptations. To provide the greatest possible spread of spore sizes, additional large-spored species were added to our analysis until every $10\text{-}\mu\text{m}$ interval of volumetric radii contained at least five species.

We find that the drag on a spore can be calculated by approximating its shape by an ellipsoid of matching size and aspect ratio. This applies even to spores with pointed apices, or surface decorations such as warts, spines, or ridges, because at small Reynolds numbers such shape features do not strongly contribute to drag. Four of 102 species in our phylogenetic survey have decorated surfaces. To show the validity of the approximation, we compare directly the computed drag on one smooth-spored species and three species of exceptionally rugose spores with the computed fluid drag on the corresponding ellipsoids. Rugose spore silhouettes were traced from electron micrographs: an image of the sculpted species *Aleuria aurantia* was provided by J. Dumais and images of the ridged species *Peziza baddia* and of the coarsely warty *Peziza viciinii* were taken from ref. 22, whereas the silhouette of the smooth spored species *Neurospora crassa* was traced from an optical micrograph provided by N.B. Raju (see Fig. 2). The true spore shape was approximated by revolving the silhouette to form an three-dimensional body. The computed drag on the spore is compared with the drag on its approximating ellipsoid in Table 1.

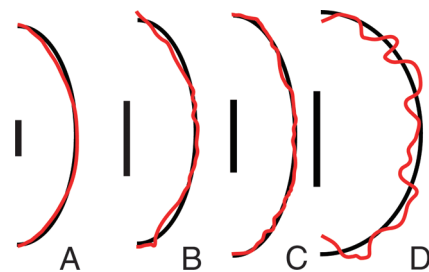


Fig. 2. Silhouettes of highly rugose spores (red curves), traced from optical or electron micrographs and approximating ellipsoids (black curves) constructed to have the same volume and aspect ratio for *N. crassa* (A), *A. aurantia* (B), *P. baddia* (C), and *P. viciinii* (D). (Scale bar: $5 \mu\text{m}$.) Although the approximating ellipsoids do not precisely capture the shape of the spore, they well-approximate the drag on the spore (see Table 1).

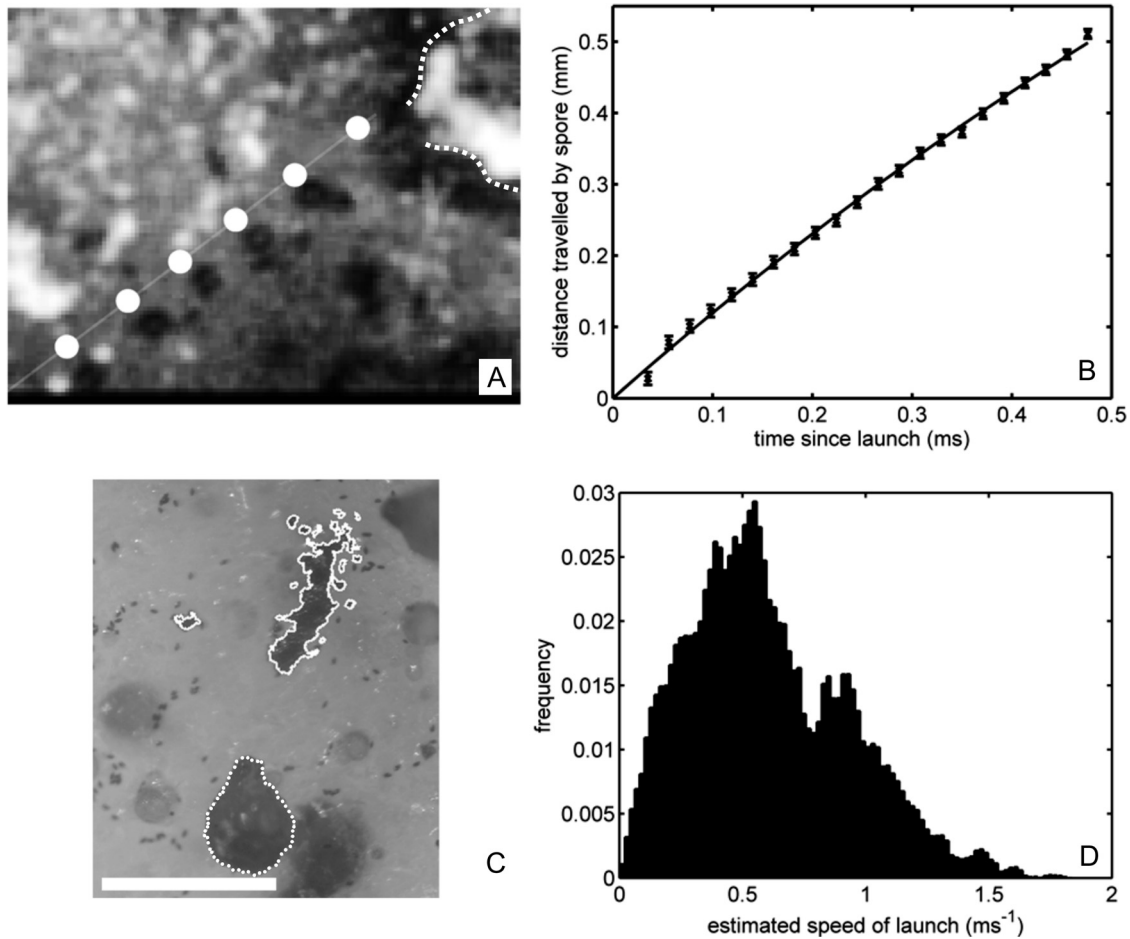


Fig. 4. Experimental determination of spore ejection speed in *N. tetrasperma*. (A) Composite image of the flight of a *N. tetrasperma* spore at 63-μs intervals, including (slightly displaced) trajectory predicted from Eq. 2. The dotted curve shows the outline of originating perithecium. (B) Fit of spore trajectory (points) to Eq. 2; giving launch speed $U_0 = 1.24 \text{ m} \cdot \text{s}^{-1}$. (C) Spore piles (outlined by solid curves) surrounding the perithecium (dotted curve). (Scale bar: 0.5 mm.) (D) Inferred launch speeds from spore prints of $N = 100$ fruiting bodies.

family Tuberales) in ref. 27. We collected spore-shape data for the type species of each of these genera, and added two additional species per genus, either drawn from the references or randomly selected from the Cybertruffle taxonomic lists (28).

Spores from both groups of nonejected species have significantly larger mean drag (one-tailed Wilcoxon signed rank test $P < 0.001$) and fewer species within 1% of the drag minimum (ejected species, 73/102; insect dispersed group, 29/65; *hypogeous* group 9/57) (see Fig. 5). The appearance of nonejected, spores with almost drag-minimizing shapes may result from the retention of an ancestral shape in the absence of selection for a new optimal shape; it is certainly for this reason that at least one species of hypogeous ascomycete (*Geopora*) still ejects its spores forcibly, albeit into the closed cavity of the fruiting body (29).

By considering the coevolution of spore size and shape over the reconstructed history of one family of fungi, we can determine the extent to which drag minimization, as opposed to other constraints, has controlled evolution of spore shape. The Pertusariaceae are a cosmopolitan medium-sized family of lichen species, most with forcibly ejected spores, and with the widest range of spore sizes of any ascomycete family (30–32).

We model the evolution of spore shape (aspect ratio α_i) and size (represented by $u_i = \log \mathcal{R}e_i$) within each Pertusariacean lineage by a stochastic process:

$$\begin{aligned} d\alpha_i(t) &= -k_\alpha(\alpha_i - \alpha^*(u_i))dt + \sigma_\alpha dW_t^{\alpha_i} \\ du_i(t) &= -k_u(u_i - u^*)dt + \sigma_u dW_t^{u_i} \end{aligned} \quad [3]$$

where dt is any scalar increment of genetic change. The first terms in the left-hand sides of Eq. 3 represent the force of selection for shapes with an optimal aspect ratio $\alpha^*(u)$, and size u^* , whereas $dW_t^{\alpha_i}$ and $dW_t^{u_i}$ are independent Wiener processes, representing the fluctuating contributions of genetic drift and other shape constraints (33). We apply the model to a two-gene phylogeny of 44 representative extant species (32). First, we find that differences in spore size and shape between species are uncorrelated with genetic distances estimated from the phylogeny ($r^2 < 1.0 \times 10^{-3}$, Mantel test $P = 0.09$), suggestive of strong recent selection (see *Materials and Methods*). We therefore use shapes drawn independently from the invariant distribution of the stochastic process (Eq. 3) to fit the model to the real spore shape data and to obtain measures of the relative contributions of drag minimization and drift to shape evolution. In particular, we estimate $\sigma_\alpha^2/2k_\alpha = 0.267$, so that in practical terms selection has dominated drift to constrain spore aspect ratio to within $\approx 25\%$ of the optimal value. Finally, by comparing the fit of the strong selection model with the fit from a drift-based reconstruction of the ancestral spore shapes (34) we confirm that the covariation of aspect ratio with size in the family is much more likely to have arisen by selection than by chance (36) (see *Materials and Methods*).

Materials and Methods

Calculation of Optimal Shapes. Shapes of projectiles that minimize drag for prescribed Reynolds number and body volume were calculated by using a gradient descent algorithm, in which successive volume-preserving perturbations were made to the shape of a suboptimal projectile (20). At each iteration

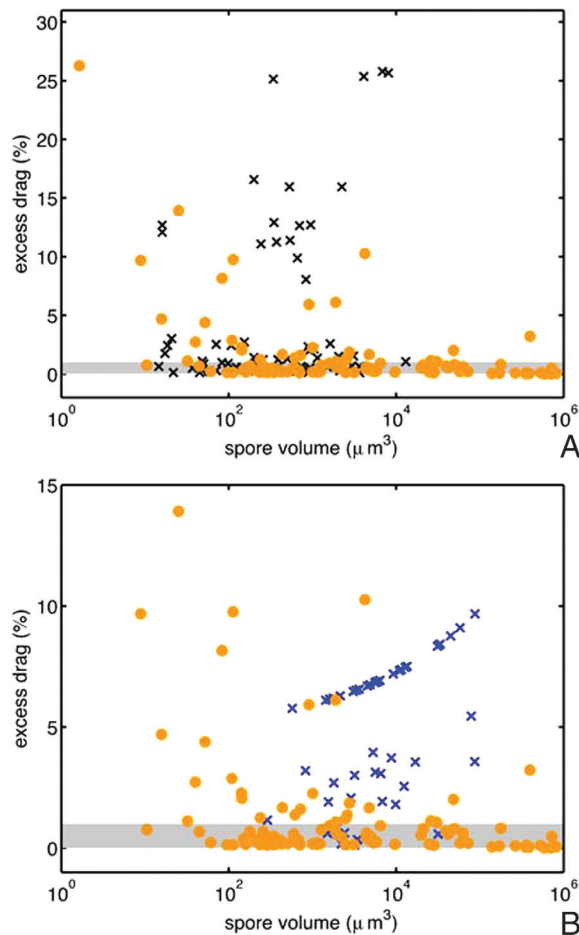


Fig. 5. Ejected and nonejected spores. (A) Comparison of excess drag—the difference in drag between the real spore shape and the optimal shape of the same size—on logarithmic axes for forcibly ejected spores (●) and (x) insect-dispersed Sordariomycete spores. (B) Comparison of excess drag for forcibly ejected spores and hypogeous Pezizomycete spores (x). Species within the shaded region have drag-to-mass ratios within 1% of the optimal value. More than 75% of forcibly ejected spores, but <45% of insect dispersed spores and 16% of hypogeous spores have excess drag values below this bound. The axes have been rescaled in B, removing the ejected species *G. platystroma* from the plot window.

we calculated the change in fluid drag due to an arbitrary perturbation to the body boundary, and then inferred the optimal perturbation. Specifically, for a body, Ω , immersed in an infinite fluid domain, we calculate the effect of a small perturbation to the shape boundary, $\partial\Omega$, on the drag-functional:

$$L[\Omega] = \int_{\partial\Omega} \mathbf{n} \cdot \boldsymbol{\sigma} \cdot \mathbf{U} dS + \int_{\mathbb{R}^3 - \Omega} [\mathbf{w} \cdot (\nabla \cdot \boldsymbol{\sigma} - \rho(\mathbf{u} \cdot \nabla)\mathbf{u}) + q \nabla \cdot \mathbf{u}] dV + \lambda \left(\int_{\Omega} dV - |\Omega| \right). \quad [4]$$

The first term of the of the functional represents the rate of working of the drag force on the body, the adjoint velocity (\mathbf{w}) and pressure (q) fields are Lagrange multipliers that, respectively, enforce conservation of momentum and incompressibility in the surrounding fluid, and the Lagrange multiplier λ enforces volume conservation. Deformations to the boundary of the body are constructed as surface functions $\alpha(x)$ giving the local normal shift of the boundary from x to $x + \alpha(x)\mathbf{n}$. Provided that the adjoint fields satisfy an equation:

$$-\nabla q + \eta \nabla^2 \mathbf{w} = -\rho(\mathbf{u} \cdot \nabla)\mathbf{w} + \rho(\mathbf{U}_j + \mathbf{w}_j) \nabla u_j, \quad [5]$$

with $\nabla \cdot \mathbf{w} = 0$, subject to boundary conditions $\mathbf{w} = \mathbf{0}$ on the boundary of the shape and $\mathbf{w} \rightarrow -\mathbf{U}$ in the far-field, then the corresponding small change in total drag on the body can be cast as a single integral over the unperturbed surface:

$$\delta L = - \int_{\partial\Omega} \alpha(x) \left(\eta \frac{\partial \mathbf{u}}{\partial n} \frac{\partial \mathbf{w}}{\partial n} + \lambda \right) dS. \quad [6]$$

We can then write down the perturbation of the shape boundary that achieves maximum drag reduction while fixing the volume of the shape:

$$\alpha(x) \propto \eta \frac{\partial \mathbf{u}}{\partial n} \frac{\partial \mathbf{w}}{\partial n} - \frac{\eta}{|\partial\Omega|} \int_{\partial\Omega} \frac{\partial \mathbf{u}}{\partial n} \frac{\partial \mathbf{w}}{\partial n} dS, \quad [7]$$

in which λ has been chosen to ensure that $\int_{\partial\Omega} \alpha dS = 0$, so that the volume of the body is preserved. A parameter μ is introduced to parameterize the sequence of shapes that the body passes through to reach the drag minimum, giving an equation $\alpha\mu \equiv dx/d\mu$, which is integrated by using a low-order variable step-size routine (the Matlab function `ode23`). At each step the Navier–Stokes flow equations and adjoint Eq. 5 are solved numerically by discretizing the velocity and adjoint velocity field (\mathbf{u}, \mathbf{w}) by quadratic finite elements, and (p, q) by linear finite elements on an unstructured triangular mesh, and solving the discretized system by using COMSOL Multiphysics. Computation of optimal shapes is computationally costly, so we interpolate from the aspect ratio and drag data for exact optimal shapes at a small set of values of $\mathcal{R}e$ to intermediate values of $\mathcal{R}e$, by approximating the minimum-drag body by the least-drag *spindle* formed by rotating the arc of a circle around the associated chord, and carrying out a single-parameter search over chord to width ratios (see *SI Appendix I*).

Measurement of Launch Speed. Launch speed was directly measured in *N. tetrasperma* (Strain no. 614, obtained from the Fungal Genetics Stock Center), cultured in 10-cm-diameter Petri dishes in crossing medium at 1% sucrose concentration (37). Petri dishes were stacked, and the stacks laid in a container with a slotted lid, to control the direction of incident light, and illuminated for 10 min per day. On the ninth day of incubation cultures used for spore print photography were abraded with a cotton-tipped applicator to remove conidia and aerial mycelia. Photographs were taken 11 days after inoculation. Cultures used for high-speed imaging were deprived of light from the eighth day onward. High-speed imaging was carried out on the tenth day after inoculation. Petri dishes were righted, conidia removed, and ejection imaged at magnifications of up to 40x, and frame rates of up to 50,000 fps by using a Phantom v7 camera mounted on a Olympus SZX-ILLB2-100 dissecting scope. Even a small misalignment of initial trajectory and focal plane causes the spores to leave the plane of focus. However, 40 h of imaging sufficed to capture 30 ejection events and one focused sequence of images of a launched spore.

Comparative Methods. We infer the relative strengths of drag minimization and drift as shape determinants by fitting the invariant distribution of the stochastic process (Eq. 3) to real spore shape data. Over the range of spore sizes covered by the Pertusariaceae ($0.5 < \log \mathcal{R}e < 2.3$), the optimal aspect ratio varies approximately linearly with u : $\alpha^*(u) = \alpha_0 + \alpha_1 u$, where $\alpha_0 = 2.02$ and $\alpha_1 = 0.38$. Eq. 3 therefore defines an Ornstein–Uhlenbeck process with Gaussian invariant distribution (35), so that the spore shapes of tip species are independent random variables with expectation and covariance matrices

$$\mathcal{E} \begin{pmatrix} \alpha_i \\ u_i \end{pmatrix} = \begin{pmatrix} \alpha^*(u^*) \\ u^* \end{pmatrix} \\ \mathcal{E} \begin{pmatrix} \alpha_i^2 & \alpha_i' u_i' \\ \alpha_i' u_i' & u_i'^2 \end{pmatrix} = \frac{1}{4k_u k_\alpha - k_\alpha^2 \alpha_1^2} \begin{pmatrix} 2\sigma_\alpha^2 k_u & \alpha_1 \sigma_\alpha \sigma_u k_\alpha \\ \alpha_1 \sigma_\alpha \sigma_u k_\alpha & 2\sigma_u^2 k_\alpha \end{pmatrix}, \quad [8]$$

where we have defined $\alpha_i' \equiv \alpha_i - \mathcal{E}(\alpha_i)$ and $u_i' \equiv u_i - \mathcal{E}(u_i)$.

Maximum likelihood estimates for each of the parameters in the model can then be extracted from the observed first and second moments of the species

Table 2. Parameter estimators and Akaike information criteria for shape evolution models fitted to spore shape data from the Pertusariaceae

	Strong selection	Weak selection	Size selection
$\sigma_\alpha^2/2k_\alpha$	0.267	—	—
$\sigma_u^2/2k_u$	0.278	—	—
k_u/k_α	0.127	—	—
u^*	1.17	—	0.92
k_u (bp/sub.)	—	—	10.02
σ_α^2 (bp/sub.)	—	13.9	13.9
σ_u^2 (bp/sub.)	—	6.50	9.30
$\alpha(0)$	—	2.40	2.40
$u(0)$	—	1.21	2.24
$-2 \log \mathcal{L}$	119.70	131.81	128.50
AICc	128.95	141.07	143.30

Strong selection (first column), stationary distribution of Eq. 3; strong drift and no selection (second column) (Eq. 9); and selection on spore size, but no selection on shape (third column) (Eq. 10).

data. Four dimensionless parameters must be estimated, and we choose these to be u^* , $\sigma_u^2/2k_u$, $\sigma_u^2/2k_u$ and k_u/k_u (see [SI Appendix](#), Fig. S4).

The statistical support for the hypothesis of evolution of spores under strong shape selection can be determined by comparing the fit to real spore shape data from model 3 with two other models for trait evolution: (i) a Brownian model (34), in which both u and α are unconstrained:

$$\begin{aligned} d\alpha_i(t) &= \sigma_\alpha^2 dW_t^{\alpha_i} \\ du_i(t) &= \sigma_u^2 dW_t^{u_i} \end{aligned} \quad [9]$$

and (ii) a Ornstein–Uhlenbeck process in which α is unconstrained, but there is selection on the size variable u :

$$\begin{aligned} d\alpha_i(t) &= \sigma_\alpha^2 dW_t^{\alpha_i} \\ du_i(t) &= -k_u(u_i - u_*)dt + \sigma_u^2 dW_t^{u_i}. \end{aligned} \quad [10]$$

$dW_t^{\alpha_i, u_i}$ are independent Wiener processes, and t parameterizes the amount of genetic change from the common ancestor of the family. Distinct lineages co evolve from the ancestral state up until the time, $t = t_{ij}$ of first divergence, so that shape and size data for the observed species have multivariate Gaussian distributions. Thus, if t_i is the “age” of the i th lineage then for Eq. 10:

$$\begin{aligned} \mathcal{E}\alpha_i(t_i) &= \alpha_i(0) \\ \mathcal{E}u_i(t_i) &= (1 - e^{-k_u t_i})u_* + e^{-k_u t_i}u(0) \\ \text{cov}(\alpha_i(t_i), \alpha_j(t_j)) &= \sigma_\alpha^2 t_{ij}, \\ \text{cov}(u_i(t_i), u_j(t_j)) &= \frac{\sigma_u^2}{2k_u} e^{-k_u(t_i+t_j-2t_{ij})} (1 - e^{-2k_u t_{ij}}), \end{aligned} \quad [11]$$

and the corresponding distribution for the pure Brownian process Eq. 9 can be obtained by setting $k_u = 0$. A version of these formulae for the case when all lineages have the same ages ($t_i = t_j$ for all i, j) is given in ref. 36. Note that genetic and phenotypic distances between tip species will become uncorrelated if and only if $k_u \Delta t \gg 1$, where Δt is the smallest genetic distance between any pair of species, i.e., in the presence of strong selection. We measure t in units of the average number of substitutions per base pair, in the two genetic loci used in ref. 32. $\sigma_{u, \alpha}^2$ therefore have units of base pairs per substitution. Fitting these models to the observed species data requires estimation of (i) four or (ii) six parameters: the drift strengths, $\sigma_{u, \alpha}^2$, the ancestral spore shape data $[\alpha_i(0), u_i(0)]$ and, in the case of process 10, the force of selection k_u and optimal size u_* .

The maximum likelihood estimators for all the parameters that feature in the three models are given in Table 2. The Akaike Information Criterion corrected for small sample sizes (AICc) allows the quality of fit of the three models to be compared (36), and shows that the strong selection hypothesis provides a significantly better fit to the real spore shapes data than either of the models in which there is no shape selection (last row of Table 2).

ACKNOWLEDGMENTS. We thank Imke Schmitt, Jacques Dumais, and François Lutzoni for making their data available to us, Jacques Dumais, L. Mahadevan, Nicholas Money, Andrew Murray, Sheila Patek, Frances Trail, Dominic Vella, Howard Stone, and members of the Pringle lab for useful discussions and comments on the manuscript, and Ozymandias Agar for assistance with the spore launch imaging. This work was supported by fellowships from the Kodak-Eastman group and the Harvard University Herbaria (M.R.) and by additional support from the Harvard Materials Research Science and Engineering Center and National Science Foundation Division of Mathematical Sciences.

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